## **Supporting Information**

## Critical state-induced emergence of superior magnetic performances in an iron-based amorphous soft magnetic composite

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**Figure S1.** Morphology and thermal analysis of the FeSiBCCr amorphous powder. (a) SEM image and (b) DSC curve of the atomized FeSiBCCr powder under the heating rate of 40 K/min.



**Figure S2.** Characterizations of the coating layer of the ASMC. SEM images of the (a) passivated and (b) EP coating powders; (c1) Cross-sectional morphology of the coated powder; (c2-c6) Magnification of the polished cross-section and corresponding EDS images of the ASMC; (d) Cross-section of the ASMC and (e1-e6) corresponding EDS mappings. (f) FTIR spectra of the raw, passivated and coated powders; (g) XPS spectra of the raw, passivated and coated powders; (g) xPS spectra of the raw, passivated and coated powders; (g) raw and (i) insulated powders; Zoomed-in C1s peak of the (h) raw and (i) insulated powders; Zoomed-in O1s peak of the (j) raw and (k) insulated powders.



Figure S3. (a) HRTEM image of the local crystal-like order dispersed in the FeSiBCCr amorphous matrix. (b) Corresponding image after auto-correlation function transform. The distance between two fringes is ~0.2 nm, consisting with the interplanar spacing of (1 1 0) plane in  $\alpha$ -Fe phase.

Figure S4(a) shows the HRTEM image of the original FeSiBCCr amorphous powder, exhibiting a typical maze-like pattern without detectable crystalline structure. Figure S4(b) presents the 2D-ACF segments of the region in figure S4(a). The areal fraction of critical structures marked by red and green squares are 11.3%.



**Figure S4.** (a) HRTEM image and (b) corresponding 2D-ACF mappings of the as-atomized FeSiBCCr amorphous powder, each cell with a size of  $1.01 \times 1.01$  nm<sup>2</sup>.

Figure S5 displays the temperature dependence of  $M_s$  and  $\mu_e$  of the FeSiBCCr SMCs. It can be seen that both  $M_s$  and  $\mu_e$  obtain maximum values at the 475-RFA, corresponding to the critical-state amorphous powder.



Figure S5. Variations of  $M_s$  and  $\mu_e$  of the FeSiBCCr SMCs annealed under different conditions



Figure S6. Frequency dependence of quality factor (Q) for the annealed ASMCs

To clarify the effect of annealing treatment on  $P_{cv}$ , loss separation was carried out. In general, the total magnetic core loss  $P_{cv}$  of ASMCs can be divided into three parts: hysteresis loss ( $P_h$ ), eddy current loss ( $P_e$ ) and residual loss ( $P_r$ ) as depicted by Eq. (1) [1].

$$P_{cv} = P_h + P_e + P_{ex} = K_h B_m^n f + K_e B_m^2 f^2 + K_r B_m^{1.5} f^{1.5}$$
(1)

Where,  $K_h$ ,  $K_e$  and  $K_r$  denote hysteresis, eddy current and excess loss coefficients, and  $B_m$ , f are magnetic flux density and frequency. Among them,  $P_r$  originates from relaxation and resonance losses and is usually negligible at low and ultra-high frequencies [2,3]. As displayed in figure S7(a),  $P_{cv}/f$  versus f can be well fitted by linear function, indicating the  $P_{cv}$  of the studied FeSiBCCr ASMCs is mainly composed of  $P_h$  and  $P_e$ . Therefore, the  $P_{cv}$  in this study is expressed by Eq. (2). The loss separation was performed according to the equation.





**Figure S7.** (a) The relationship between frequency and  $P_{cv}/f$  and (b) corresponding loss separation of the ASMCs annealed at different temperatures



Figure S8. Variation of P<sub>cv</sub>, P<sub>h</sub> and P<sub>e</sub> from 75 kHz to 1 MHz for the 475-RFA ASMCs.

Figure S9 shows the MFM image of the FeSiBCCr SMC annealed at 500-RFA. Although some large-scale crystals precipitate in amorphous matrix, the magnetic domain exhibits typical strip feature, and thus the 500-RFA SMC possess better magnetic softness compared with the original SMC, i.e., higher  $\mu_e$  and lower  $P_{cv}$ .



Figure S9. 3D-MFM image of the 500-RFA SMC.

## References

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